

© International Baccalaureate Organization 2024

All rights reserved. No part of this product may be reproduced in any form or by any electronic or mechanical means, including information storage and retrieval systems, without the prior written permission from the IB. Additionally, the license tied with this product prohibits use of any selected files or extracts from this product. Use by third parties, including but not limited to publishers, private teachers, tutoring or study services, preparatory schools, vendors operating curriculum mapping services or teacher resource digital platforms and app developers, whether fee-covered or not, is prohibited and is a criminal offense.

More information on how to request written permission in the form of a license can be obtained from <https://ibo.org/become-an-ib-school/ib-publishing/licensing/applying-for-a-license/>.

© Organisation du Baccalauréat International 2024

Tous droits réservés. Aucune partie de ce produit ne peut être reproduite sous quelque forme ni par quelque moyen que ce soit, électronique ou mécanique, y compris des systèmes de stockage et de récupération d'informations, sans l'autorisation écrite préalable de l'IB. De plus, la licence associée à ce produit interdit toute utilisation de tout fichier ou extrait sélectionné dans ce produit. L'utilisation par des tiers, y compris, sans toutefois s'y limiter, des éditeurs, des professeurs particuliers, des services de tutorat ou d'aide aux études, des établissements de préparation à l'enseignement supérieur, des fournisseurs de services de planification des programmes d'études, des gestionnaires de plateformes pédagogiques en ligne, et des développeurs d'applications, moyennant paiement ou non, est interdite et constitue une infraction pénale.

Pour plus d'informations sur la procédure à suivre pour obtenir une autorisation écrite sous la forme d'une licence, rendez-vous à l'adresse <https://ibo.org/become-an-ib-school/ib-publishing/licensing/applying-for-a-license/>.

© Organización del Bachillerato Internacional, 2024

Todos los derechos reservados. No se podrá reproducir ninguna parte de este producto de ninguna forma ni por ningún medio electrónico o mecánico, incluidos los sistemas de almacenamiento y recuperación de información, sin la previa autorización por escrito del IB. Además, la licencia vinculada a este producto prohíbe el uso de todo archivo o fragmento seleccionado de este producto. El uso por parte de terceros —lo que incluye, a título enunciativo, editoriales, profesores particulares, servicios de apoyo académico o ayuda para el estudio, colegios preparatorios, desarrolladores de aplicaciones y entidades que presten servicios de planificación curricular u ofrezcan recursos para docentes mediante plataformas digitales—, ya sea incluido en tasas o no, está prohibido y constituye un delito.

En este enlace encontrará más información sobre cómo solicitar una autorización por escrito en forma de licencia: <https://ibo.org/become-an-ib-school/ib-publishing/licensing/applying-for-a-license/>.

**Mathematics: applications and interpretation**  
**Higher level**  
**Paper 1**

1 May 2024

**Zone A** afternoon | **Zone B** afternoon | **Zone C** afternoon

Candidate session number

2 hours

--	--	--	--	--	--	--	--	--	--

**Instructions to candidates**

- Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- A graphic display calculator is required for this paper.
- Answer all questions.
- Answers must be written within the answer boxes provided.
- Unless otherwise stated in the question, all numerical answers should be given exactly or correct to three significant figures.
- A clean copy of the **mathematics: applications and interpretation HL formula booklet** is required for this paper.
- The maximum mark for this examination paper is **[110 marks]**.



Answers must be written within the answer boxes provided. Full marks are not necessarily awarded for a correct answer with no working. Answers must be supported by working and/or explanations. Solutions found from a graphic display calculator should be supported by suitable working. For example, if graphs are used to find a solution, you should sketch these as part of your answer. Where an answer is incorrect, some marks may be given for a correct method, provided this is shown by written working. You are therefore advised to show all working.

1. [Maximum mark: 9]

Imani invests \$3000 in a bank that pays a nominal annual interest rate of 1.25% compounded monthly.

- (a) Calculate the amount of money Imani will have in the bank at the end of 6 years. Give your answer correct to two decimal places. [3]
- (b) Calculate the number of months it takes until Imani has at least \$3550 in the bank. [2]

Imani uses the \$3550 as a partial payment for a used car costing \$22 000. For the remainder she takes out a loan from a bank.

- (c) Write down the amount of money that Imani takes out as a loan. [1]

The loan is for 8 years and the nominal annual interest rate is 12.6% compounded monthly. Imani will pay the loan in fixed monthly instalments at the end of each month.

- (d) Calculate the amount, correct to the nearest dollar, that Imani will have to pay the bank each month. [3]

**(This question continues on the following page)**











5. [Maximum mark: 8]

The annual growth of a tree is 80% of its growth during the previous year.

This year the tree is 42 m in height and one year ago its height was 37 m.

(a) Calculate the annual growth of the tree in the coming year. [2]

(b) Calculate the height of the tree 6 years from now. Give your answer correct to the nearest cm. [4]

If the tree continues to follow this pattern of growth, its height will never exceed  $k$  metres.

(c) Find the smallest possible value of  $k$ . [2]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....





6. [Maximum mark: 6]

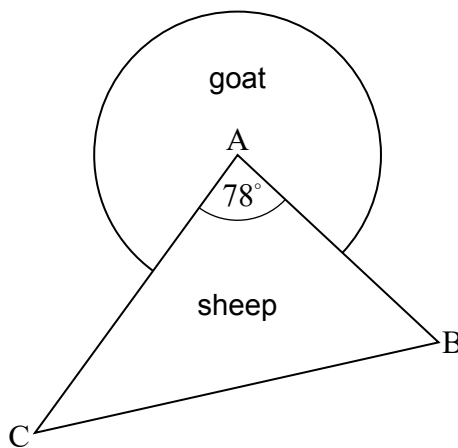
A sheep is in a field in the shape of a triangle, ABC.

$AC = 21$  metres,  $AB = 15$  metres and  $\hat{CAB} = 78^\circ$ .

A goat is in an adjacent field in the shape of a sector of a circle with centre, A, and radius 8 metres.

The fields are shown in the diagram.

**diagram not to scale**



Determine which animal, the sheep or the goat, is in the field with the larger area, and state how many extra square metres are in this larger field.

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....





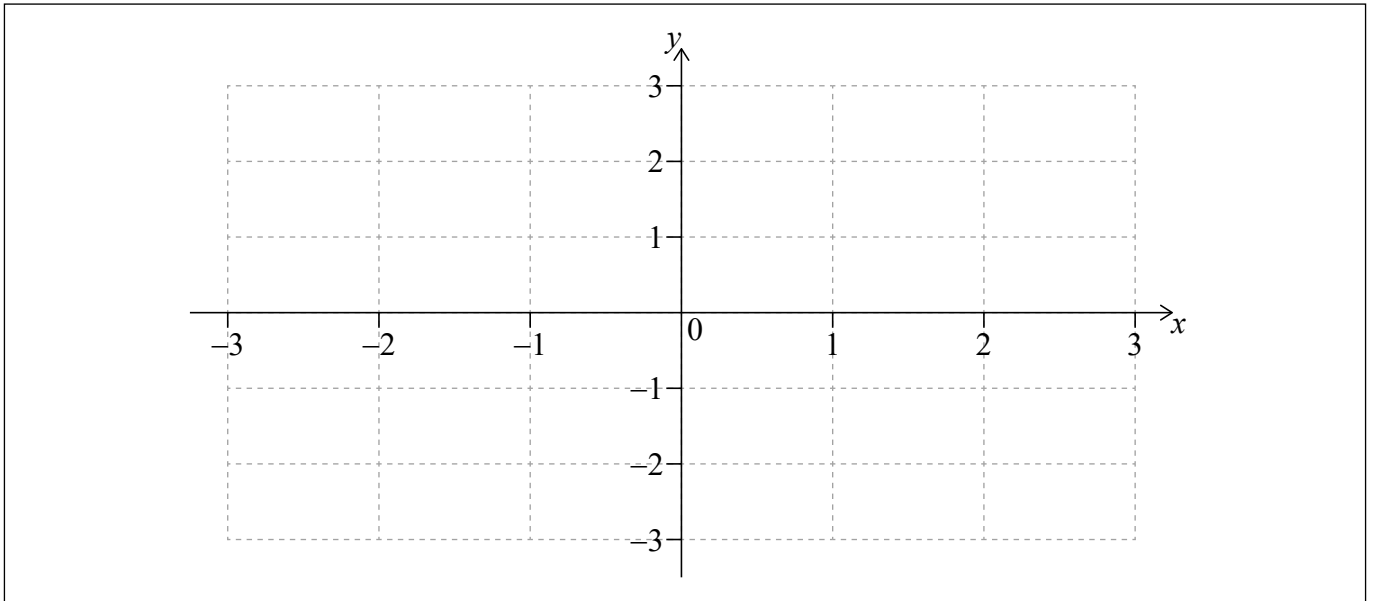


10. [Maximum mark: 9]

Consider the function  $f(x) = x\sqrt{3-x^2}$ ,  $-\sqrt{3} \leq x \leq \sqrt{3}$ .

(a) Sketch the graph of  $y = f(x)$  on the following pair of axes.

[2]



The area between the graph of  $y = f(x)$  and the  $x$ -axis is rotated through  $360^\circ$  about the  $x$ -axis.

(b) (i) Write down an integral that represents this volume.

(ii) Calculate the value of this integral.

[4]

The graph of the function  $f$  is transformed, to give the graph of the function  $g$ , in the following way:

- It is first stretched by scale factor 2, parallel to the  $x$ -axis with the  $y$ -axis invariant.
- It is then stretched by scale factor 0.5, parallel to the  $y$ -axis with the  $x$ -axis invariant.

(c) Find the volume obtained when the area between the graph of  $y = g(x)$  and the  $x$ -axis is rotated through  $360^\circ$  about the  $x$ -axis.

[3]

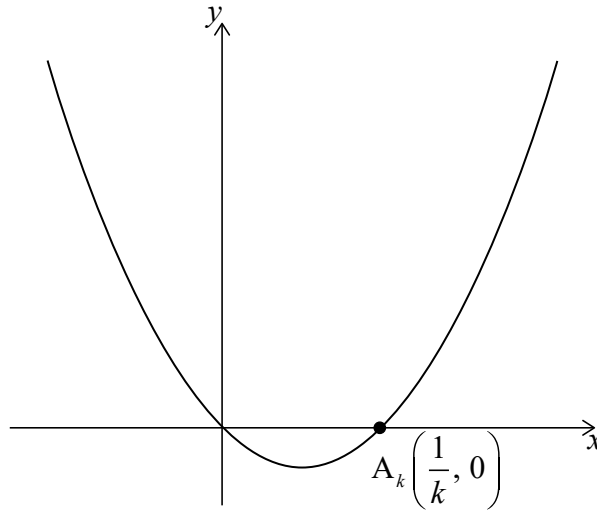
(This question continues on the following page)





11. [Maximum mark: 9]

The diagram shows the curve with equation  $y_k = kx^2 - x$ ,  $k > 0$ , which intersects the  $x$ -axis at the origin and at the point  $A_k\left(\frac{1}{k}, 0\right)$ .



The normal to the curve at  $A_k$  intersects the curve again at point  $B_k$ .

- (a) Show that the  $x$ -coordinate of  $B_k$  is  $-\frac{1}{k}$ . [6]

Consider the case where  $k = 2$ .

- (b) Calculate the finite area of the region between the curve with equation  $y_2 = 2x^2 - x$  and the normal at  $A_2$ . [3]

(This question continues on the following page)















Please **do not** write on this page.

Answers written on this page  
will not be marked.



20EP20